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using Robust Control

Technique

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Performance Investigation of a Permanent Magnet DC Machines using Robust Control Technique

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Abstract

In this paper, the design and performance investigation of the permanent magnet machines have been done to increase the mechanical and electrical outputs improvement of the systems. A permanent magnet Dc motor (PMDM) and generator (PMDG) have been modelled and designed to improve the angular position and generated current respectively. In this work, augmentation based H₂ optimal and H_{∞} synthesis controllers have been designed as a controller for the two systems and a comparison between the proposed controller for tracking a reference inputs and a promising results have been obtained.

Keywords: Permanent magnet Dc motor, Permanent magnet Dc generator, H₂ optimal controller, H_{∞} synthesis controllers

1. Introduction

The permanent magnet machines have the benefit of getting an excitation from the permanent magnet which is found at the stator part of the machines in order to get some efficiency benefit for that. Induction machines have a good and regulated fluxes that's why it is helpful to optimize the efficiency. Both systems are used for variable-speed drive. The specification of the performance and efficiency of the permanent magnet machine better has better cost minimization function with optimal for the range and performance target. In this paper, the modeling design and control of a permanent magnet Dc motor and generator for improving the angular speed and generating current have been done using robust control theory.

2. Mathematical Modelling

2.1 Permanent Magnet DC Motor Modelling

Consider the cross section of a motor shown in Figure 1 below that has several loops of wire.

Figure 1 PMDM cross section

The static magnetic field formed by a electromagnet with strength β going from left to right (North to South). The thickness of the magnet is defined by ℓ . The loops of the wire around a "rotor" which is an iron cylinder with radius "a" that is free to rotate about its center. There are "n" rounds of wire with current going into the page on the right side, and comes out of the page to the right). The rotational angle, θ , is positive in the clockwise direction, the resistance of the wire is given by R . The moment of inertia of the rotor, " J ," with friction of rotation " B_r ." The mathematical model for this system is derived by separating the system as mechanical system and the electrical system as shown in Figure 2 below.

Figure 2 Mechanical and electrical systems

The torque developed in the loop of wire is given by

$$\tau_e = 2nail\beta = \alpha i \quad (1)$$

$$\alpha = 2nal\beta$$

With a back emf

$$e_m = 2n\omega al\beta = \alpha\omega \quad (2)$$

The electrical source is the input to the and the mechanical torque is the output of the motor
From the mechanical body diagram we get

$$J\ddot{\theta} + B_r\dot{\theta} = \tau_e = \alpha i \quad (3)$$

and from the electrical free diagram we get

$$e_{in} - iR = e_m = \alpha\omega \quad (4)$$

Substituting Equation (3) for current into Equation (4) yields:

$$e_{in} - \frac{J\ddot{\theta} + B_r\dot{\theta}}{\alpha} R = \alpha\omega = \alpha\dot{\theta} \quad (5)$$

Taking the Laplace transform with initial conditions set to zero and solve for the ratio of output to input yields:

$$\frac{\Theta(s)}{E_{in}(s)} = \frac{\alpha}{JR s^2 + (B_r R + \alpha^2)s}$$

The parameters of the PMDM is shown in Table 1 below.

Table 1 PMDM parameters

No	Parameter	Symbol	Value
1	Resistance of the Wire	R	10 ohm
2	Moment of inertia of the rotor	J	$0.8 \text{ Kg m}^2 / \text{s}^2$
3	Friction of rotation	B_r	1.2 Nms
	Motor specification	α	1.8

The transfer function numerically becomes

$$\frac{\Theta(s)}{E_{in}(s)} = \frac{1}{4.44s^2 + 8.47s}$$

2.2 Permanent Magnet DC Generator Modelling

A permanent magnet DC generator is typically the same machine as a motor. The motor uses a mechanical input and generates an electrical output.

Figure 3 PMDG cross section

The free body diagram of the mechanical and electrical system is shown in Figure 4 below. In this system consideration of the direction of the induced torque is essential. The positive current is coming out of the page on the left side of the rotor and the field is to the right. The back emf, is in the positive direction with counterclockwise direction of the wires on the left side have positive velocity downward.

Figure 4 Mechanical and electrical systems

$$\begin{aligned} \tau_e + \tau_{in} + J\dot{\omega} &= 0 \\ \alpha i + \tau_{in} + J\dot{\omega} &= 0 \end{aligned} \quad (6)$$

$$\begin{aligned} e_m + iR &= 0 \\ \alpha\omega + iR &= 0 \end{aligned} \quad (7)$$

Taking the Laplace Transform of Equation (6) and Equation (7) and eliminating the angular velocity, $\omega(s)$ yields:

$$\frac{I(s)}{T_{in}(s)} = \frac{\alpha}{JR s + \alpha^2}$$

The parameters of the PMDG is shown in Table 2 below.

Table 2 PMDG parameters

No	Parameter	Symbol	Value
1	Resistance of the Wire	R	15 ohm
2	Moment of inertia of the rotor	J	$0.6 \text{ Kg m}^2 / \text{s}^2$
3	Motor specification	α	2.9

The transfer function numerically becomes

$$\frac{I(s)}{T_{in}(s)} = \frac{1}{3.1s + 2.9}$$

3. Proposed Controllers Design

3.1 Augmentations of the Model with Weighting Functions

The weighted control structure of the systems is shown in Figure 5, where $W1(s)$, $W2(s)$, and $W3(s)$ are weighting functions. The assumption that $G(s)$, $W1(s)$, and $W3(s)$ are all proper systems. The weighting function $W3(s)$ is not required to be proper system. In the state space structure of the systems, the output vector $y1 = [y1a, y1b, y1c]^T$ cannot be used directly to the control signal u . Clearly, Figure 5 represents a more general picture of optimal and robust control systems. The design of the H_2 optimal and H_∞ synthesis controllers is done by using the idea of the augmented state space model.

Figure 5 weighted control structure with the proposed controllers

For the motor

The weighting function $W1m(s)$, $W2m(s)$, and $W3m(s)$ are chosen as

$$W_{1m}(s) = \frac{s+1}{2s+5} \quad W_{2m}(s) = \frac{s+8}{3s+24} \quad W_{3m}(s) = 7$$

The H_2 optimal controller become

$$G_{mH_2} = \frac{3.1679s^2 + 11.3466s + 41.7504}{s^3 + 47.1659s^2 + 125.7358s + 28.2287}$$

The H_∞ synthesis controller become:

$$G_{mH_\infty} = \frac{3.26s^2 + 12.2s + 28.38}{s^3 + 47.2s^2 + 128.6s + 27.6}$$

For the generator

The weighting function $W1g(s)$, $W2g(s)$, and $W3g(s)$ are chosen as

$$W_{1g}(s) = \frac{s+4}{s+8} \quad W_{2g}(s) = \frac{s+12}{2s+14} \quad W_{3g}(s) = 9$$

The H_2 optimal controller become

$$G_{gH_2} = \frac{2.5736s + 12.0904}{s^2 + 5.2298s + 18.7438}$$

The H_∞ synthesis controller become:

$$G_{gH_\infty} = \frac{3.2096s + 18.3848}{s^2 + 8.6176s + 17.4376}$$

4. Result and Discussion

4.1 Comparison of a PMDM with H₂ Optimal and H_{∞} Synthesis Controllers for Improving the Angular Position using a Step Reference Angular Position Input

The angular position output of a PMDM performance analysis is done by simulating the system with the proposed controllers for a step input reference input and the simulation result is shown in Figure 6 below.

Figure 6 Step response of the PMDM

The simulation result shows that the PMDM with H₂ optimal controller improves the angular position in minimizing the percentage overshoot and the settling time better than the system with H_{∞} synthesis controller.

4.2 Comparison of a PMDM with H₂ Optimal and H_{∞} Synthesis Controllers for Improving the Angular Position using a Random Reference Angular Position Input

The angular position output of a PMDM performance analysis is done by simulating the system with the proposed controllers for a random input reference input and the simulation result is shown in Figure 7 below.

Figure 7 Random response of the PMDM

The simulation result shows that the PMDM with H 2 optimal controller improves the angular position in tracking the reference input signal with better amplitude than the system with H^∞ synthesis controller.

4.3 Comparison of a PMDM with H 2 Optimal and H^∞ Synthesis Controllers for Improving the Generating Current using a Step Reference Current Input

The angular position output of a PMDM performance analysis is done by simulating the system with the proposed controllers for a step input reference input and the simulation result is shown in Figure 8 below.

Figure 8 Step response of the PMDG

The simulation result shows that the PMDM with H 2 optimal controller improves the generating current in minimizing the percentage overshoot better than the system with H^∞ synthesis controller.

4.4 Comparison of a PMDM with H 2 Optimal and H^∞ Synthesis Controllers for Improving the Generating Current using a Random Reference Current Input

The angular position output of a PMDM performance analysis is done by simulating the system with the proposed controllers for a random input reference input and the simulation result is shown in Figure 9 below.

Figure 9 Random response of the PMDG

The simulation result shows that the PMDG with H_2 optimal controller improves the angular position in tracking the reference input signal with better amplitude than the system with H_∞ synthesis controller.

5. Conclusion

The modelling, design and control of a permanent magnet Dc motor for an improvement of angular position and a permanent magnet Dc generator for improving of the generating current using augmentation based H_2 optimal and H_∞ synthesis controllers. A comparison of the proposed systems with the proposed controllers for the analysis of the performance improvement of the angular position and generating current using a step and random reference input signals. The simulation result of the PMDM for a step reference angular position input suggested that the PMDM with H_2 optimal controller improves the angular position in minimizing the percentage overshoot and the settling time while the simulation result of the PMDM for a random reference angular position suggested that the PMDM with H_2 optimal controller improves the angular position in tracking the reference input signal with better amplitude. The simulation results of the PMDG suggested that the PMDG with H_2 optimal controller improves the generating current in minimizing the percentage overshoot for a step input reference current and the PMDG with H_2 optimal controller improves the angular position in tracking the reference input signal with better amplitude.

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