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# Normalization and variance stabilization of single-cell RNA-seq data using regularized negative binomial regression

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## Abstract

Single-cell RNA-seq (scRNA-seq) data exhibits significant cell-to-cell variation due to technical factors, including the number of molecules detected in each cell, which can confound biological heterogeneity with technical effects. To address this, we present a modeling framework for the normalization and variance stabilization of molecular count data from scRNA-seq experiments. We propose that the Pearson residuals from “regularized negative binomial regression,” where cellular sequencing depth is utilized as a covariate in a generalized linear model, successfully remove the influence of technical characteristics from downstream analyses while preserving biological heterogeneity. Importantly, we show that an unconstrained negative binomial model may overfit scRNA-seq data, and overcome this by pooling information across genes with similar abundances to obtain stable parameter estimates. Our procedure omits the need for heuristic steps including pseudocount addition or log-transformation and improves common downstream analytical tasks such as variable gene selection, dimensional reduction, and differential expression. Our approach can be applied to any UMI-based scRNA-seq dataset and is freely available as part of the R package `sctransform`, with a direct interface to our single-cell toolkit `Seurat`.

**Keywords:** Single-cell RNA-seq, Normalization

## Introduction

In the analysis and interpretation of single-cell RNA-seq (scRNA-seq) data, effective pre-processing and normalization represent key challenges. While unsupervised analysis of single-cell data has transformative potential to uncover heterogeneous cell types and states, cell-to-cell variation in technical factors can also confound these results [1, 2]. In particular, the observed sequencing depth (number of genes or molecules detected per cell) can vary significantly between cells, with variation in molecular counts potentially spanning an order of magnitude, even within the same cell type [3]. Importantly, while the now widespread use of unique molecular identifiers (UMI) in scRNA-seq removes technical variation associated with PCR, differences in cell lysis, reverse transcription efficiency, and stochastic molecular

sampling during sequencing also contribute significantly, necessitating technical correction [4]. These same challenges apply to bulk RNA-seq workflows, but are exacerbated due to the extreme comparative sparsity of scRNA-seq data [5].

The primary goal of single-cell normalization is to remove the influence of technical effects in the underlying molecular counts, while preserving true biological variation. Specifically, we propose that a dataset which has been processed with an effective normalization workflow should have the following characteristics:

- 1 In general, the normalized expression level of a gene should not be correlated with the total sequencing depth of a cell. Downstream analytical tasks (dimensional reduction, differential expression) should also not be influenced by variation in sequencing depth.
- 2 The variance of a normalized gene (across cells) should primarily reflect biological heterogeneity, independent of gene abundance or sequencing depth.

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For example, genes with high variance after normalization should be differentially expressed across cell types, while housekeeping genes should exhibit low variance. Additionally, the variance of a gene should be similar when considering either deeply sequenced cells, or shallowly sequenced cells.

Given its importance, there have been a large number of diverse methods proposed for the normalization of scRNA-seq data [6–11]. In general, these fall into two distinct sets of approaches. The first set aims to identify “size factors” for individual cells, as is commonly performed for bulk RNA-seq [12]. For example, BASiCS [7] infers cell-specific normalizing constants using spike-ins, in order to distinguish technical noise from biological cell-to-cell variability. Scran [8] pools cells with similar library sizes and uses the summed expression values to estimate pool-based size factors, which are resolved to cell-based size factors. By performing a uniform scaling per cell, these methods assume that the underlying RNA content is constant for all cells in the dataset and that a single scaling factor can be applied for all genes.

Alternative normalization approaches model molecule counts using probabilistic approaches. For example, initial strategies focused on read-level (instead of UMI-level) data and modeled the measurement of each cell as a mixture of two components: a negative binomial (NB) “signal” component and a Poisson “dropout” component [13]. For newer measurements based on UMI, modeling strategies have focused primarily on the use of the NB distribution [14], potentially including an additional parameter to model zero-inflation (ZINB). For example, ZINB-WaVE [9] models counts as ZINB in a special variant of factor analysis. scVI and DCA also use the ZINB noise model [10, 15], either for normalization and dimensionality reduction in Bayesian hierarchical models or for a denoising autoencoder. These pioneering approaches extend beyond pre-processing and normalization, but rely on the accurate estimation of per-gene error models.

In this manuscript, we present a novel statistical approach for the modeling, normalization, and variance stabilization of UMI count data for scRNA-seq. We first show that different groups of genes cannot be normalized by the same constant factor, representing an intrinsic challenge for scaling-factor-based normalization schemes, regardless of how the factors themselves are calculated. We instead propose to construct a generalized linear model (GLM) for each gene with UMI counts as the response and sequencing depth as the explanatory variable. We explore potential error models for the GLM and find that the use of unconstrained NB or ZINB models leads to overfitting of scRNA-seq data and a significant dampening of biological variance. To address this, we find that by pooling information across genes

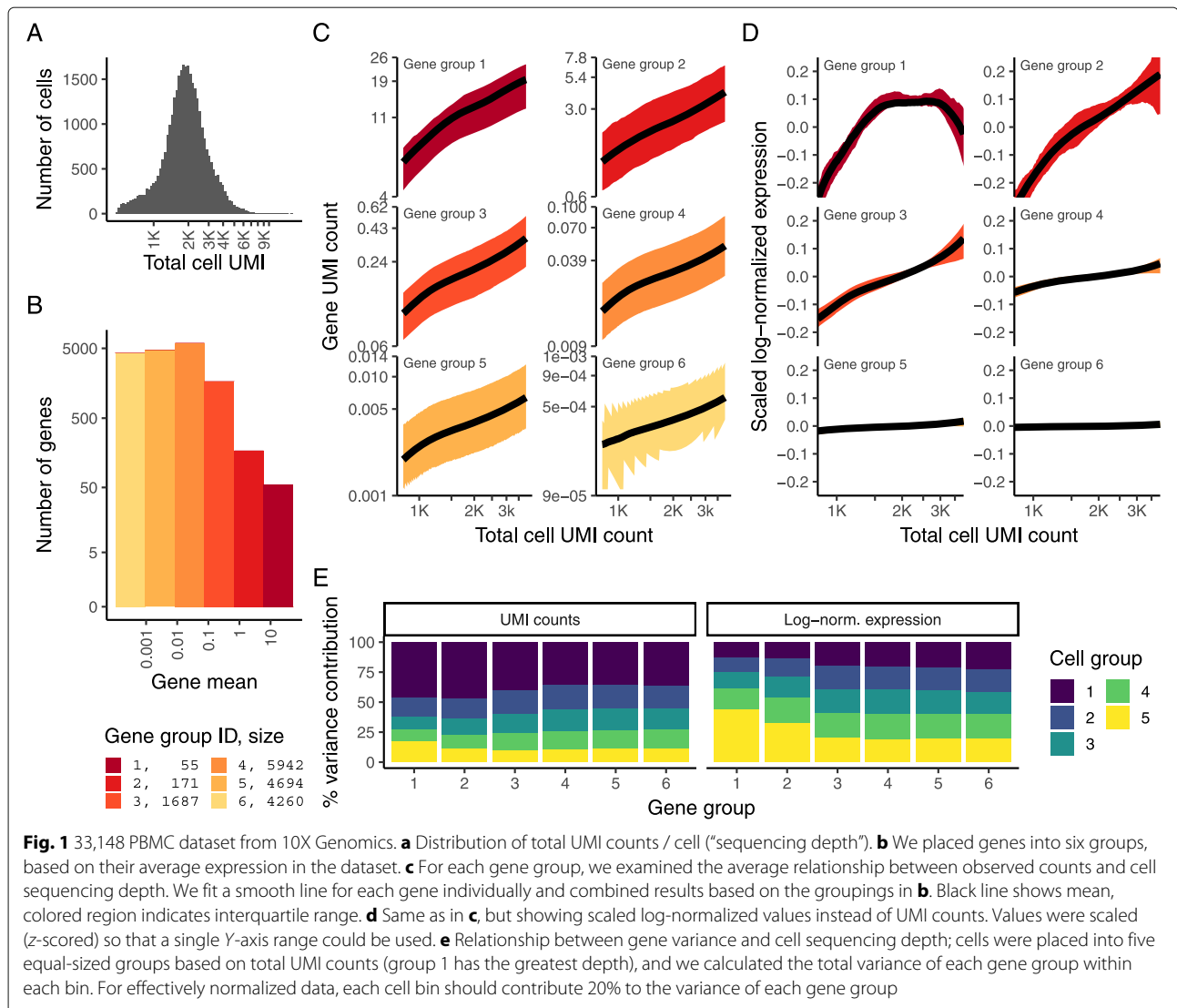
with similar abundances, we can regularize parameter estimates and obtain reproducible error models. The residuals of our “regularized negative binomial regression” represent effectively normalized data values that are no longer influenced by technical characteristics, but preserve heterogeneity driven by distinct biological states. Lastly, we demonstrate that these normalized values enable downstream analyses, such as dimensionality reduction and differential expression testing, where the results are not confounded by cellular sequencing depth. Our procedure is broadly applicable for any UMI-based scRNA-seq dataset and is freely available to users through the open-source R package `sctransform` ([github.com/ChristophH/sctransform](https://github.com/ChristophH/sctransform)), with a direct interface to our single-cell toolkit `Seurat`.

## Results

### A single scaling factor does not effectively normalize both lowly and highly expressed genes

Sequencing depth variation across single cells represents a substantial technical confounder in the analysis and interpretation of scRNA-seq data. To explore the extent of this effect and possible solutions, we examined five UMI datasets from diverse tissues, generated with both plate- and droplet-based protocols. We show results on all datasets in Additional file 1, but focus here on a dataset of 33,148 human peripheral blood mononuclear cells (PBMC) freely available from 10x Genomics. This dataset is characteristic of current scRNA-seq experiments; we observed a median total count of 1891 UMI/cell and observed 16,809 genes that were detected in at least 5 cells (Fig. 1a, b). As expected, we observed a strong linear relationship between unnormalized expression (gene UMI count) and cellular sequencing depth. We observed nearly identical trends (and regression slopes) for genes across a wide range of abundance levels, after grouping genes into six equal-width bins based on their mean abundance (Fig. 1c), demonstrating that counts from both low- and high-abundance genes are confounded by sequencing depth and require normalization.

We next tested how the standard normalization approach in popular scRNA-seq packages such as `Seurat` [16–18] and `SCANPY` [19] compensates for this effect. In this two-step process (referred to as “log-normalization” for brevity), UMI counts are first scaled by the total sequencing depth (“size factors”) followed by pseudocount addition and log-transformation. While this approach mitigated the relationship between sequencing depth and gene expression, we found that genes with different overall abundances exhibited distinct patterns after log-normalization, and only low/medium-abundance genes in the bottom three tiers were effectively normalized (Fig. 1d). In principle, this confounding relationship could be driven by the presence of multiple cell



types in human PBMC. However, when we analyzed a 10X Chromium dataset that used human brain RNA as a control (“Chromium control dataset” [5]), we observed identical patterns, and in particular, ineffectual normalization of high-abundance genes (Additional file 1: Figure S1 and S2).

Moreover, we also found that gene variance was also confounded with sequencing depth. We quantified this phenomenon by binning cells by their overall sequencing depth and quantifying the total variance of each gene group within each bin. For effectively normalized data, we expect uniform variance across cell groups, but we observed substantial imbalances in the analysis of log-normalized data. In particular, cells with low total UMI counts exhibited disproportionately higher variance for high-abundance genes, dampening the variance contribution from other gene groups (Fig. 1e). We also tested

an alternative to log-normalization (“relative counts” normalization), where we simply divided counts by total sequencing depth. Removing the log-transformation mitigated the relationships between gene expression, gene variance, and sequencing depth, but residual effects remained in both cases (Additional file 2: Figure S1).

These results demonstrate inherent challenges for “size factor”-based normalization strategies. Notably, while recent normalization strategies leverage more advanced strategies to learn cell “size factors” [7, 20], the use of a single factor will introduce distinct effects on different gene sets, given their average abundance. This suggests that genes may require normalization strategies that depend on their abundance level. Indeed, the authors of SCnorm [6] reached similar conclusions in the normalization of non-UMI-based single-cell RNA-seq data. Their method utilizes quantile regression to treat distinct gene

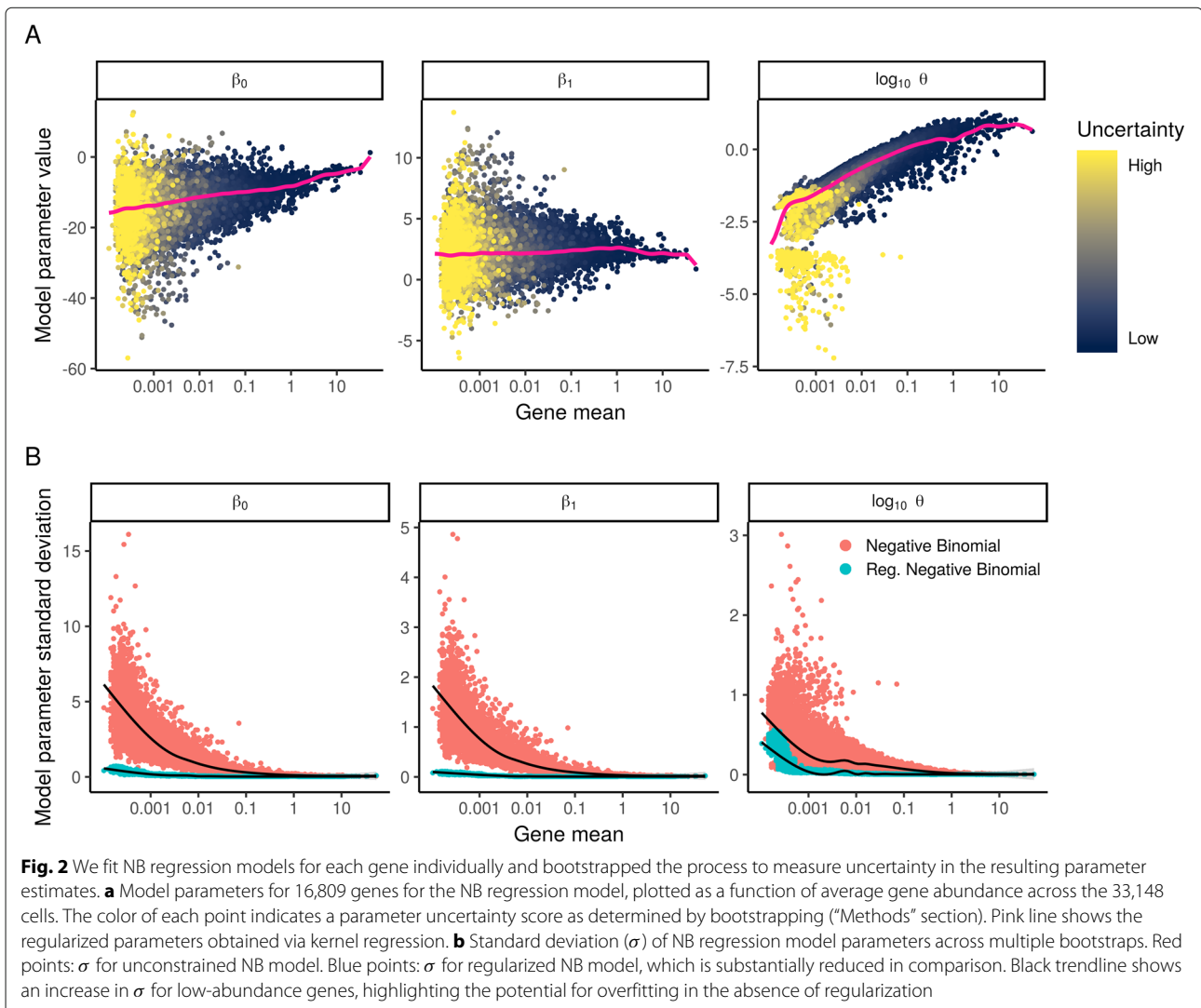
groups separately, but ignores zero values which predominantly characterize droplet-based scRNA-seq. We therefore explored alternative solutions based on statistical modeling of the underlying count data.

### Modeling single-cell data with a negative binomial distribution leads to overfitting

We considered the use of generalized linear models as a statistical framework to normalize single-cell data. Motivated by previous work that has demonstrated the utility of GLMs for differential expression [21, 22], we reasoned that including sequencing depth as a GLM covariate could effectively model this technical source of variance, with the GLM residuals corresponding to normalized expression values. The choice of a GLM error model is an important consideration, and we first tested the use of a negative binomial distribution, as has been proposed for overdispersed single-cell count data [9, 14], performing “negative

binomial regression” (“Methods” section) independently for each gene. This procedure learns three parameters for each gene, an intercept term  $\beta_0$  and the regression slope  $\beta_1$  (influence of sequencing depth), which together define the expected value, and the dispersion parameter  $\theta$  characterizing the variance of the negative binomial errors.

We expected that we would obtain consistent parameter estimates across genes, as sequencing depth should have similar (but not identical as shown above) effects on UMI counts across different loci. To our surprise, we observed significant heterogeneity in the estimates of all three parameters, even for genes with similar average abundance (Fig. 2). These differences could reflect true biological variation in the distribution of single-cell gene expression, but could also represent irreproducible variation driven by overfitting in the regression procedure. To test this, we bootstrapped the analysis by repeatedly fitting



a GLM to randomized subsets of cells and assessed the variance of parameter estimates. We found that parameter estimates were not reproducible across bootstraps (Fig. 2), particularly for genes with low to moderate expression levels, and observed highly concordant results when estimating uncertainty using the GLM fisher information matrix as an alternative to bootstrapping (see the “Methods” section and Additional file 2: Figure S2). We repeated the same analysis on the “Chromium control dataset,” where the data from each droplet represents a technical replicate of a bulk RNA sample. There is no biological variation in this sample, but parameters from negative binomial regression still exhibited substantial variation across genes, particularly for lowly abundant genes (Additional file 2: Figure S3). Taken together, these results demonstrate that the gene-specific differences we observed were exaggerated due to overfitting.

Our observation that single-cell count data can be overfit by a standard (two-parameter) NB distribution demonstrates that additional constraints may be needed to obtain robust parameter estimates. We therefore considered the possibility of constraining the model parameters through regularization, by combining information across similar genes to increase robustness and reduce sampling variation. This approach is commonly applied in learning error models for bulk RNA-seq in the context of differential expression analysis [22–25], but to our knowledge has not been previously applied in this context for single-cell normalization. We note that in contrast to our approach, the use of a zero-inflated negative binomial model requires an additional (third) parameter, exacerbating the potential for overfitting. We therefore suggest caution and careful consideration when applying unconstrained NB or ZINB models to scRNA-seq UMI count data.

To address this challenge, we applied kernel regression (“Methods” section) to model the global dependence between each parameter value and average gene expression. The smoothed line (pink line in Fig. 2) represents a regularized parameter estimate that can be applied to constrain NB error models. We repeated the bootstrap procedure and found that in contrast to independent gene-level estimates, regularized parameters were consistent across repeated subsamples of the data (Fig. 2b), suggesting that we are robustly learning the global trends that relate intercept, slope, and dispersion to average gene expression.

Our regularization procedure requires the selection of a kernel bandwidth, which controls the degree of smoothing. We used a data-based bandwidth selection method [26] scaled by a user-defined bandwidth adjustment factor. In Additional file 2: Figure S4, we show that our method returns robust results when varying this parameter within a reasonable range that extends over an order of magnitude, but that extreme values

result in over/under-smoothing which will have adverse effects.

### Applying regularized negative binomial regression for single-cell normalization

Our observations above suggest a statistically motivated, robust, and efficient process to normalize single-cell data. First, we utilize generalized linear models to fit model parameters for each gene in the transcriptome (or a representative subset; Additional file 2: Figure S7; “Methods” section) using sequencing depth as a covariate. Second, we apply kernel regression to the resulting parameter estimates in order to learn regularized parameters that depend on a gene’s average expression and are robust to sampling noise. Finally, we perform a second round of NB regression, constraining the parameters of the model to be those learned in the previous step (since the parameters are fixed, this step reduces to a simple affine transformation; “Methods” section). We treat the residuals from this model as normalized expression levels. Positive residuals for a given gene in a given cell indicate that we observed more UMIs than expected given the gene’s average expression in the population and cellular sequencing depth, while negative residuals indicate the converse. We utilize the Pearson residuals (response residuals divided by the expected standard deviation), effectively representing a variance-stabilizing transformation (VST), where both lowly and highly expressed genes are transformed onto a common scale.

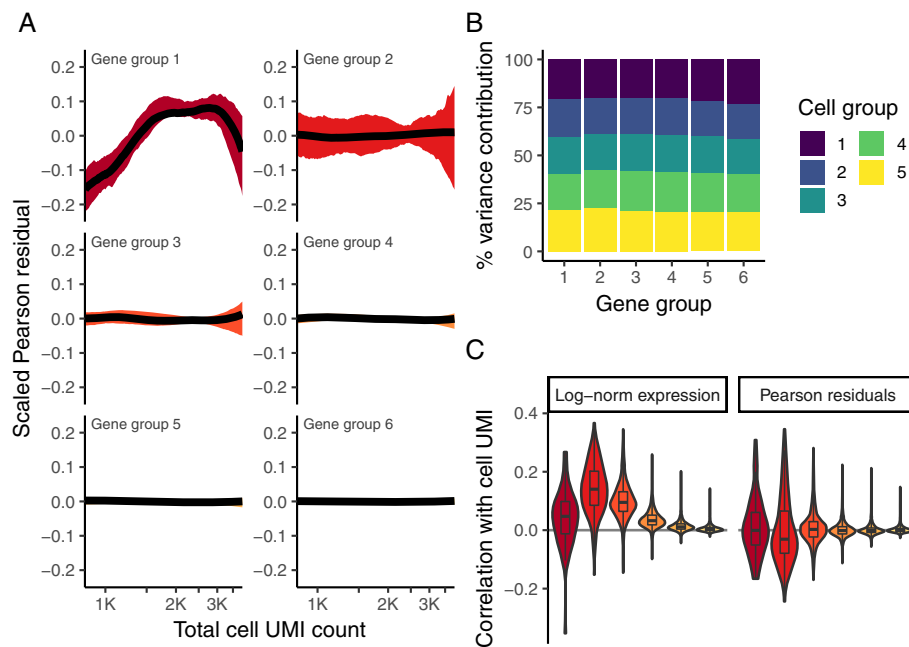
This workflow also has attractive properties for processing single-cell UMI data, including:

- 1 We do not assume a fixed “size,” or expected total molecular count, for any cell.
- 2 Our regularization procedure explicitly learns and accounts for the well-established relationship [27] between a gene’s mean abundance and variance in single-cell data
- 3 Our VST is data driven and does not involve heuristic steps, such as a log-transformation, pseudocount addition, or z-scoring.
- 4 As demonstrated below, Pearson residuals are independent of sequencing depth and can be used for variable gene selection, dimensional reduction, clustering, visualization, and differential expression.

### Pearson residuals effectively normalize technical differences, while retaining biological variation

To evaluate our regularized NB regression model, we explored the relationship between the Pearson residuals and cellular sequencing depth. Encouragingly, we observed minimal correlation (Fig. 3a, c), for genes across the full range of expression levels. In addition, gene variance was strikingly consistent across cells with different





**Fig. 3** Pearson residuals from regularized NB regression represent effectively normalized scRNA-seq data. Panels **a** and **b** are analogous to Fig. 1 **d** and **e**, but calculated using Pearson residuals. **c** Boxplot of Pearson correlations between Pearson residuals and total cell UMI counts for each of the six gene bins. All three panels demonstrate that in contrast to log-normalized data, the level and variance of Pearson residuals is independent of sequencing depth

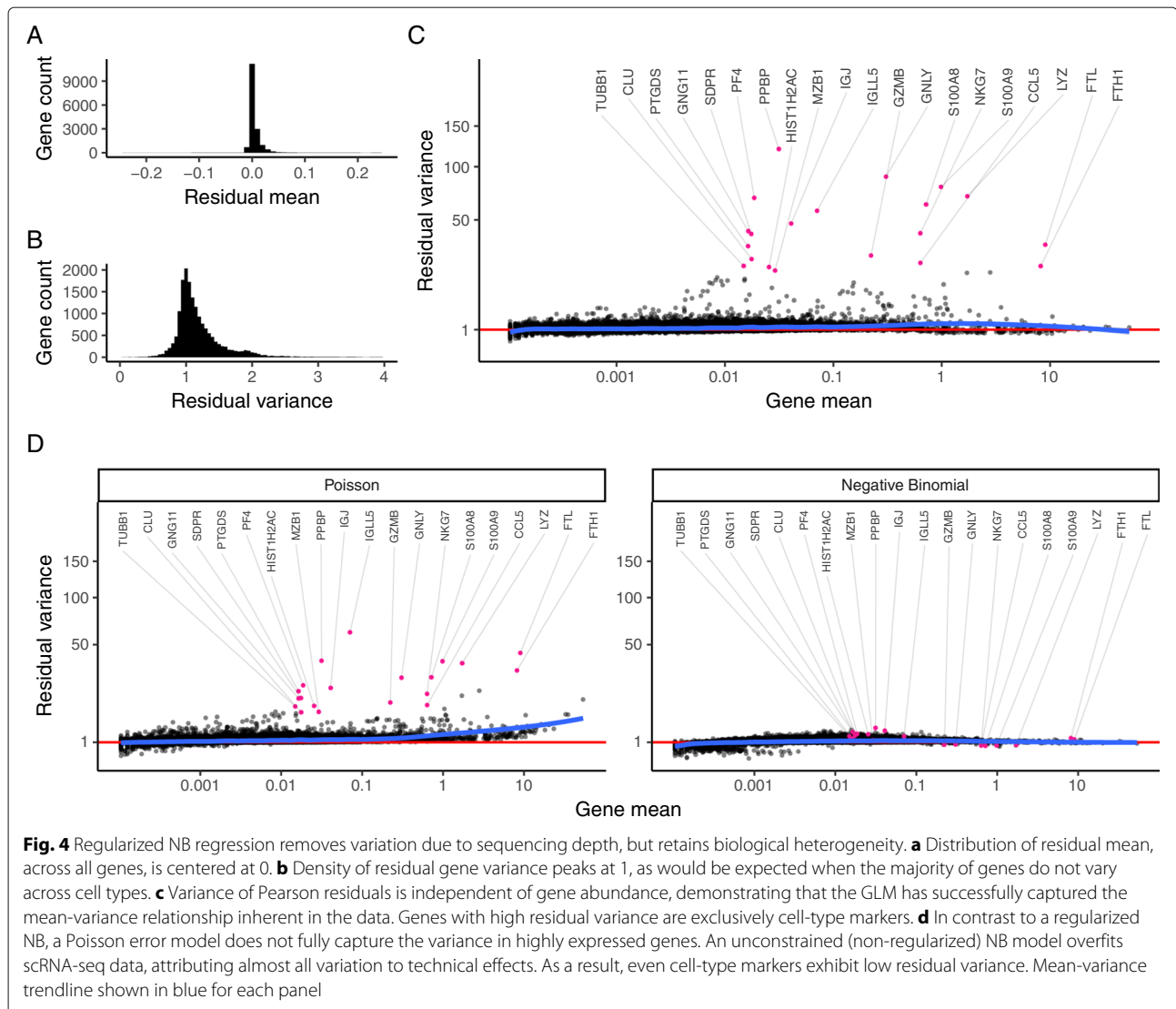
sequencing depths (Fig. 3b, contrast to Fig. 1e), with no evidence of expression “dampening” as we observed when using a cell-level size factor approaches. Taken together, these results suggest that our Pearson residuals represent effectively standardized expression values that are not influenced by technical metrics.

Our model predicts that for genes with minimal biological heterogeneity in the data (i.e., genes whose variance is driven primarily by differences in sequencing depth), residuals should be distributed with a mean of zero and unit variance. We observe these values for the majority of genes in the dataset (Fig. 4a, b), demonstrating effective and consistent variance stabilization across a range of expression values (Fig. 4c). However, we observed a set of outlier genes with substantially higher residual variance than predicted by our background model, suggesting additional biological sources of variation in addition to sampling noise. Further exploration of these genes revealed that they exclusively represent markers of known immune cell subsets (e.g., PPBP in Megakaryocytes, GNLY in NK cells, IGJ in plasma cells). We repeated the analysis after subsampling the number of cells in the dataset (Additional file 2: Figure S5) and also on the “Chromium control dataset.” Reassuringly, for the control dataset, we did not observe genes with high residual variance (Additional file 2: Figure S3), demonstrating that our model correctly ascribed all variation in this control

dataset to technical sources. Finally, we performed a simulation study to evaluate the sensitivity of our method to detect variable genes (Additional file 2: Figure S6). In summary, our regularized NB regression model successfully captures and removes variance driven by technical differences, while retaining biologically relevant signal. The variance of Pearson residuals correlates with biological heterogeneity and can be used to identify “highly variable” genes in single-cell data.

Our previous analyses suggest that the use of a regularized NB error model is crucial to the performance of our workflow. To test this, we substituted both a Poisson and an unconstrained NB error model into our GLM and repeated the procedure (Fig. 4d). When applying standard negative binomial regression, we found that the procedure strikingly removed both technical and biological sources of variation from the data, driven by overfitting of the unconstrained distribution. A single-parameter Poisson model performed similarly to our regularized NB, but we observed that residual variances exceeded one for all moderately and highly expressed genes. This is consistent with previous observations in both bulk and single-cell RNA-seq that count data is overdispersed [9, 12, 14, 28].

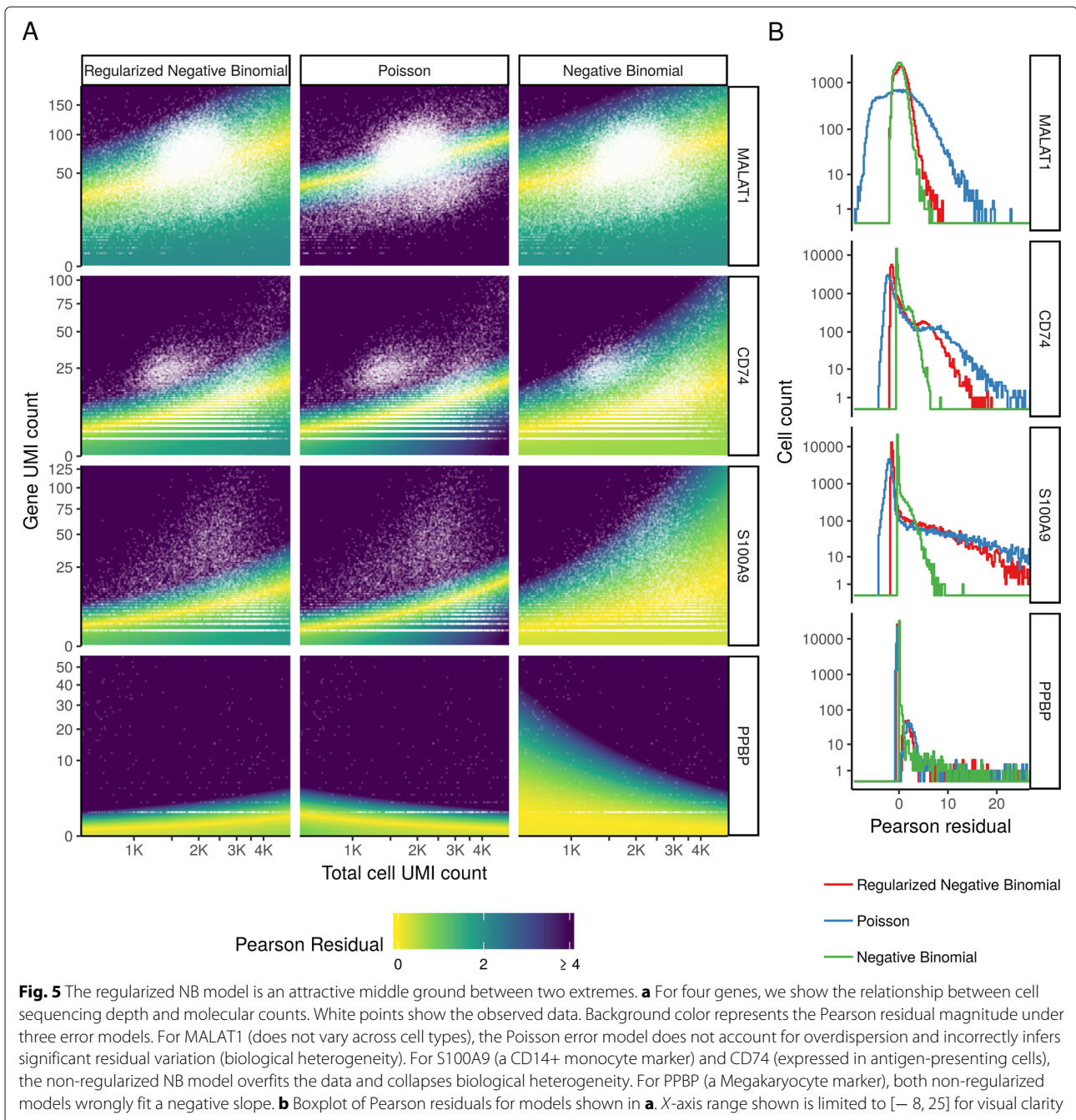
In addition to global analyses, it is also instructive to explore how each model performs on characteristic genes in the dataset. In Fig. 5, we show observed molecular counts for four representative loci, as a function of total



cell UMI count. Background colors indicate GLM Pearson residual values using three different error models (Poisson, NB, regularized NB), enabling us to explore how well each model fits the data. For MALAT1, a highly expressed gene that should not vary across immune cell subsets, we observe that both the unconstrained and regularized NB distributions appropriately modeled technically driven heterogeneity in this gene, resulting in minimal residual biological variance. However, the Poisson model does not model the overdispersed counts, incorrectly suggesting significant biological heterogeneity. For S100A9 (a marker of myeloid cell types) and CD74 (expressed in antigen-presenting cells), the regularized NB and Poisson models both return bimodally distributed Pearson residuals, consistent with a mixture of myeloid and lymphoid cell types present in blood, while the unconstrained NB collapses this biological heterogeneity via overfitting. We observe similar results

for the Megakaryocyte (Mk) marker PPBP, but note that both non-regularized models actually fit a negative slope relating total sequencing depth to gene molecule counts. This is because Mk cells have very little RNA content and therefore exhibit lower UMI counts compared to other cell types, even independent of stochastic sampling. However, it is nonsensical to suggest that deeply sequenced Mk cells should contain less PPBP molecules than shallowly sequenced Mk cells, and indeed, regularization of the slope parameter overcomes this problem.

Taken together, our results demonstrate that the regularized negative binomial represents an attractive middle ground between two extremes. By allowing for overdispersion, the model can correctly account for the variance in count data observed in single-cell assays. However, by placing data-driven constraints on the slope, intercept, and dispersion of NB regression, we substantially alleviate the problem of overfitting and ensure that biological



variation is retained after normalization. We observed identical results when considering any of the five UMI datasets we tested, including both plate- and droplet-based protocols (Additional file 1), demonstrating that our procedure can apply widely to any UMI-based scRNA-seq experiment.

#### Downstream analytical tasks are not biased by sequencing depth

Our procedure is motivated by the desire to standardize expression counts so that differences in cellular

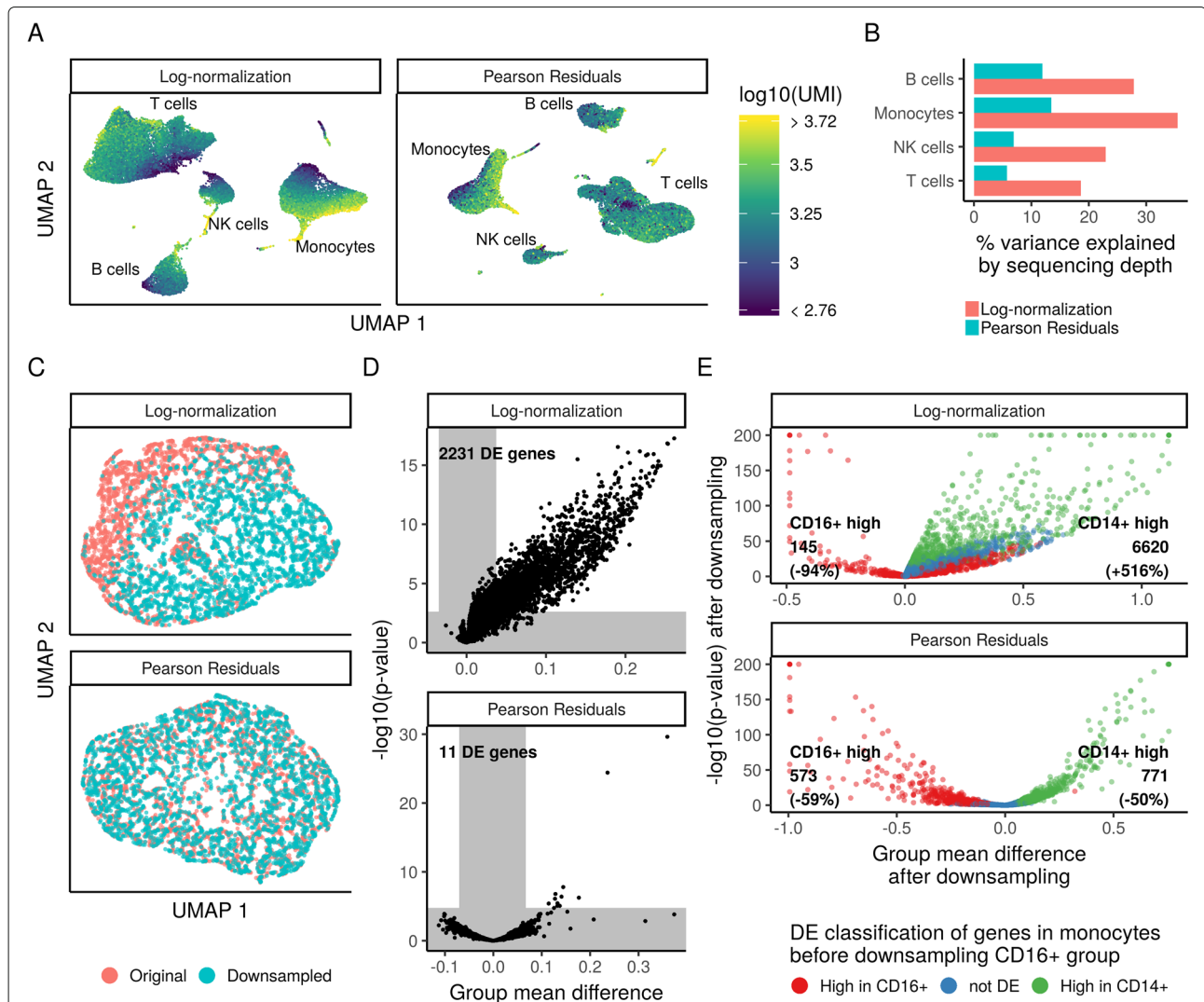
sequencing depth do not influence downstream analytical tasks. To test our performance towards this goal, we performed dimensionality reduction and differential expression tests on Pearson residuals after regularized NB regression. For comparison, we used log-normalized data. We first applied PCA followed by UMAP embedding (“Methods” section) to the full PBMC dataset, using normalized values (Pearson residuals, or log-normalized data) for all genes in the transcriptome as input to PCA, and then visualized the total number of molecules per cell on the UMAP embedding. Both normalization



schemes reveal significant biological heterogeneity in PBMC (Fig. 6a), consistent with the expected major and minor human immune cell subsets. However, the low-dimensional representation of log-normalized data was confounded by cellular sequencing depth, as both the PCA and UMAP embeddings exhibited strong correlations with this technical metric. These correlations are strikingly reduced for Pearson residuals (Fig. 6a). We note that we do not expect complete independence of biological and technical effects, as distinct cell subsets will likely vary in size and RNA content. However, even

when limiting our analyses within individual cell types, we found that cell sequencing depth explained substantially reduced variation in Pearson residuals compared to log-normalized data (Fig. 6b), consistent with our earlier observations (Fig. 3).

Imperfect normalization can also confound differential expression (DE) tests for scRNA-seq, particularly if global differences in normalization create DE false positives for many genes. To demonstrate the scope of this problem and test its potential resolution with Pearson residuals, we took CD14+ monocytes (5551 cell subset of the 33K



**Fig. 6** Downstream analyses of Pearson residuals are unaffected by differences in sequencing depth. **a** UMAP embedding of the 33,148 cell PBMC dataset using either log-normalization or Pearson residuals. Both normalization schemes lead to similar results with respect to the major and minor cell populations in the dataset. However, in analyses of log-normalized data, cells within a cluster are ordered along a gradient that is correlated with sequencing depth. **b** Within the four major cell types, the percent of variance explained by sequencing depth under both normalization schemes. **c** UMAP embedding of two groups of biologically identical CD14+ monocytes, where one group was randomly downsampled to 50% depth. **d** Results of differential expression (DE) test between the two groups shown in **c**. Gray areas indicate expected group mean difference by chance and a false discovery rate cutoff of 1%. **e** Results of DE test between CD14+ and CD16+ monocytes, before and after randomly downsampling the CD16+ cells to 20% depth

PBMC data) and randomly divided them into two groups. In one of the groups (50% of the cells), we randomly subsampled UMIs so that each cell expressed only 50% of its total UMI counts. Therefore, the two groups of monocytes are biologically equivalent and differ only in their technical sequencing depth, and we should ideally detect no differentially expressed genes between them. However, when performing DE on log-normalized data ( $t$  test with significance thresholds determined by random sampling, see the “Methods” section), we detected more than 2000 DE genes (FDR threshold 0.01), due to global shifts arising from improper normalization (Fig. 6c, d). When performing DE on Pearson residuals, we identified only 11 genes. While these 11 represent false positives, they are each highly expressed genes for which it is difficult to obtain a good fit during the regularization process as there are few genes with similar mean values (Fig. 3a top left).

We also tested a second scenario where true DE genes could be masked by sequencing depth differences. We compared two distinct populations, CD14+ and CD16+ monocytes (5551 and 1475 cells), before and after randomly downsampling the CD16+ group to 20% sequencing depth. We would expect the set of DE genes to be nearly identical in the two analyses, though we expect a decrease in sensitivity after downsampling. However, when using log-normalized data, we observed dramatic changes in the set of DE genes—with some CD14+-enriched markers even incorrectly appearing as CD16+-enriched markers after downsampling. When performing DE on Pearson residuals, the results of the two analyses were highly concordant, albeit with reduced statistical power after downsampling (Fig. 6e). Therefore, Pearson residuals resulting from regularized NB regression effectively mitigate depth-dependent differences in dimensionality reduction and differential expression, which are key downstream steps in single-cell analytical workflows.

## Discussion

Here, we present a statistical approach for the normalization and variance stabilization of single-cell UMI datasets. In contrast to commonly applied normalization strategies, our workflow omits the use of linear size/scaling factors and focuses instead on the construction of a GLM relating cellular sequencing depth to gene molecule counts. We calculate the Pearson residuals of this model, representing a variance-stabilization transformation that removes the inherent dependence between a gene’s average expression and cell-to-cell variation. In this manuscript, we demonstrate that our normalization procedure effectively removes the influence of technical variation, without dampening biological heterogeneity.

When exploring error models for the GLM, our analyses revealed that an unconstrained negative binomial model tends to overfit single-cell RNA-seq data,

particularly for genes with low/medium abundance. We demonstrate that a regularization step, a common step in bulk RNA-seq analysis [22, 28] where parameter estimates are pooled across genes with similar mean abundance, can effectively overcome this challenge and yield reproducible models. Importantly, statistical and deep-learning methods designed for single-cell RNA-seq data often utilize a negative binomial (or zero-inflated negative binomial) error model [10, 15]. Our results suggest that these and future methods could benefit by substituting a regularized model and that including an additional parameter for zero-inflation could exacerbate the risk of overfitting. More generally, our work indicates that a regularized negative binomial is an appropriate distribution to model UMI count data from a “homogeneous” cell population.

To facilitate users applying these methods to their own datasets, our approach is freely available as an open-source R package `sctransform` ([github.com/ChristophH/sctransform](https://github.com/ChristophH/sctransform)), with an accompanying interface to our single-cell R toolkit `Seurat` [16–18]. In a single command, and without any requirement to set user-defined parameters, `sctransform` performs normalization, variance stabilization, and feature selection based on a UMI-based gene expression matrix. We demonstrate the ease-of-use for `sctransform` in a short vignette analyzing a 2700 PBMC dataset produced by 10x Genomics in Additional file 3. In this example, `sctransform` reveals significant additional biological substructure in NK, T, B, and monocyte populations that cannot be observed in the standard `Seurat` workflow, which is based on log-normalization (Additional file 3).

As our workflow leverages all genes (or a random subset) for the initial regularization, we make an implicit assumption that the majority of genes in the dataset do not exhibit significant biological variation. This is analogous to similar assumptions made for bulk RNA-seq normalization and DE (i.e., that the majority of genes are not differentially expressed across conditions) [28]. While this assumption may be overly simplistic when performing scRNA-seq on a highly heterogeneous sample, we did not observe adverse effects when applying our model to human PBMC data, or any of the other datasets we examined. In principle, an extension of `sctransform` that included an initial pre-clustering step (as proposed in [8]) could alleviate this concern, as the biological heterogeneity would be significantly reduced in each group.

Our work makes extensive use of Pearson residuals, the output of our regularized NB regression procedure. These can be utilized as input for standard downstream methods, i.e., Wilcoxon rank test for differential expression, or PCA for dimensional reduction. An alternative approach, however, would modify the underlying methods themselves to assume a statistical error model that

is tailored to single-cell data. For example, Townes et al. [29] introduced GLM-PCA, a generalization of PCA for data exhibiting non-normal error distributions such as the negative binomial, that takes count data directly as input instead of relying on intermediate residuals. Similarly, an extension of `sctransform` could perform differential expression directly on the resulting parameter estimates instead of the residual values, potentially coupling this with an empirical Bayes framework [12, 30].

Finally, while we focus here on modeling technical variation due to differences in cellular sequencing depth, we note that our approach can be easily extended to model alternative “nuisance” parameters, including cell cycle [31], mitochondrial percentage, or experimental batch, simply by adding additional covariates to the model. Indeed, we observed that a modified GLM including a batch indicator variable was sufficient to correct for technical differences arising from two profiled batches of murine bipolar cells [32], though successful application requires all cell types to share a similar batch effect (Additional file 2: Figure S8). In the future, we anticipate that similar efforts can be used to model diverse single-cell data types, including single-cell protein [33], chromatin [34], and spatial [35] data.

## Methods

### Regularized negative binomial regression

We explicitly model the UMI counts for a given gene using a generalized linear model. Specifically, we use the sum of all molecules assigned to a cell as a proxy for sequencing depth and use this cell attribute in a regression model with negative binomial (NB) error distribution and log link function. Thus, for a given gene  $i$ , we have

$$\log(\mathbb{E}(x_i)) = \beta_0 + \beta_1 \log_{10} m,$$

where  $x_i$  is the vector of UMI counts assigned to gene  $i$  and  $m$  is the vector of molecules assigned to the cells, i.e.,  $m_j = \sum_i x_{ij}$ . The solution to this regression is a set of parameters: the intercept  $\beta_0$  and the slope  $\beta_1$ . The dispersion parameter  $\theta$  of the underlying NB distribution is also unknown and needs to be estimated from the data. Here we use the NB parameterization with mean  $\mu$  and variance given as  $\mu + \frac{\mu^2}{\theta}$ .

We use a regression model for the UMI counts to correct for sequencing depth differences between cells and to standardize the data. However, modeling each gene separately results in overfitting, particularly for low-abundance genes that are detected in only a minor subset of cells and are modeled with a high variance. We consider this an overestimation of the true variance, as this is driven by cell-type heterogeneity in the sample, and not due to cell-to-cell variability with respect to the independent

variable,  $\log_{10} m$ . To avoid this overfitting, we regularize all model parameters, including the NB dispersion parameter  $\theta$ , by sharing information across genes.

The procedure we developed has three steps. In the first step, we fit independent regression models per gene. In the second step, we exploit the relationship of model parameter values and gene mean to learn global trends in the data. We capture these trends using a kernel regression estimate (`ksmooth` function in R). We use a normal kernel and first select a kernel bandwidth using the R function `bw.SJ`. We multiply this by a bandwidth adjustment factor (BAF, default value of 3, sensitivity analysis shown in Additional file 2: Fig. S4). We perform independent regularizations for all parameters (Fig. 2). In the third step, we use the regularized regression parameters to define an affine function that transforms UMI counts into Pearson residuals:

$$z_{ij} = \frac{x_{ij} - \mu_{ij}}{\sigma_{ij}},$$

$$\mu_{ij} = \exp(\beta_{0i} + \beta_{1i} \log_{10} m_j),$$

$$\sigma_{ij} = \sqrt{\mu_{ij} + \frac{\mu_{ij}^2}{\theta_i}},$$

where  $z_{ij}$  is the Pearson residual of gene  $i$  in cell  $j$ ,  $x_{ij}$  is the observed UMI count of gene  $i$  in cell  $j$ ,  $\mu_{ij}$  is the expected UMI count of gene  $i$  in cell  $j$  in the regularized NB regression model, and  $\sigma_{ij}$  is the expected standard deviation of gene  $i$  in cell  $j$  in the regularized NB regression model. Here  $\beta_{0i}$ ,  $\beta_{1i}$ , and  $\theta_i$  are the linear model parameters after regularization. To reduce the impact of extreme outliers, we clip the residuals to a maximum value of  $\sqrt{N}$ , where  $N$  is the total number of cells.

We highlight that our approach was inspired by methods developed for differential expression analysis in bulk RNA-seq data. For example, DESeq [23] uses the negative binomial distribution for read count data and links variance and mean by local regression. DESeq2 [12] extends this approach with Empirical Bayes shrinkage for dispersion estimation. Additionally, edgeR [22] introduced GLM algorithms and statistical methods for estimating biological variation on a gene-wise basis and separating it from technical variation.

### Geometric mean for genes

Our regularization approach aims to pool information across genes with similar average expression. To avoid the influence of outlier cells and respect the exponential nature of the count distributions, we consistently use the geometric mean. References to average abundance or gene mean in this work are based on the following definition of mean:

$$\exp(\text{amean}(\log(x + \epsilon))) - \epsilon,$$

with  $x$  being the vector of UMI counts of the gene,  $\bar{x}$  being the arithmetic mean, and  $\epsilon$  being a small fixed value to avoid  $\log(0)$ . After trying several values for  $\epsilon$  in the range 0.0001 to 1, and not observing significant differences in our results, we set  $\epsilon = 1$ .

### Speed considerations

`sctransform` has been optimized to run efficiently on large scRNA-seq datasets on standard computational infrastructure. For example, processing of a 3000 cell dataset takes 30 s on a standard laptop (the 33,148 cell dataset utilized in this manuscript takes 6 min).

The most time-consuming step of our procedure is the initial GLM-fitting, prior to regularization. Here, we fit  $K$  linear regression models with NB error models, where  $K$  is the total number of genes in the dataset. However, since the results of the first step are only used to learn regularized parameter estimates (i.e., the overall relationship of model parameter values and gene mean), we tested the possibility of performing this step on a random subset of genes in lieu of the full transcriptome. When selecting a subset of genes to speed up the first step, we do not select genes at random, i.e., with a uniform sampling probability, as that would not evenly cover the range of gene means. Instead, we set the probability of selecting a gene  $i$  to  $1/d(\log_{10} \bar{x}_i)$ , where  $d$  is the density estimate of all  $\log_{10}$ -transformed gene means and  $\bar{x}_i$  is the mean of UMI counts of gene  $i$ .

For different numbers of genes (ranging from 4000 to 50), we drew 13 random samples to be used in the initial step of parameter estimation. We then proceeded to generate regularized models (for all genes based on parameters learned from a gene subset) and compared the results to the case where all genes were used in the initial estimation step as well. We employed a few metrics to compare the partial analysis to the full analysis: the correlation of gene-residuals, the ranking of genes based on residual variation (most highly variable genes), and the CV of sum of squared residuals across random samples (model stability). For all metrics, we observed that using as few as 200 genes in the initial estimation closely recapitulated the full results, while using 2000 genes gave rise to virtually identical estimates (Additional file 2: Figure S7). We therefore use 2000 genes in the initial GLM-fitting step.

Additionally, we explored three methods to estimate the model parameters in the initial step. We list them here in increasing order of computational complexity.

- 1 Assume a Poisson error distribution to estimate  $\beta$  coefficients. Then, given the estimated mean vector, estimate the NB  $\theta$  parameter using maximum likelihood.

- 2 Same as above, followed by a re-estimation of  $\beta$  coefficients using a NB error model with the previously estimated  $\theta$ .
- 3 Fit a NB GLM estimating both the  $\beta$  and  $\theta$  coefficients using an alternating iteration process.

While the estimated model parameters can vary slightly between these methods, the resulting Pearson residuals are extremely similar. For example, when applying the three procedures to the 10x PBMC dataset, all pairwise gene correlations between the three methods are greater than 0.99, though the alternating iteration process is fourfold more computationally demanding. We therefore proceeded with the first method.

### Model parameter stability

To assess model parameter stability, we bootstrapped the parameter estimation and sampled from all cells with replacement 13 times. For a given gene and parameter combination, we derived an uncertainty score as follows. We used the standard deviation of parameter estimates across 13 bootstraps divided by the standard deviation of the bootstrap-mean value across all genes. Values greater or equal to one indicate high uncertainty, while values less or equal to 0.01 indicate low uncertainty.

As an alternative to bootstrapping, we also examined the 95% confidence intervals (CI) of the parameter estimates. The standard errors (SE) of the parameter estimates (based on the Fisher information matrix obtained during the estimation procedure) are taken from the output of the R function `glm` (intercept and slope) and `theta.ml` ( $\theta$ ). CI are then calculated as the estimated values  $\pm 1.96 \times SE$ .

### Trends in the data before and after normalization

We grouped genes into six bins based on  $\log_{10}$ -transformed mean UMI count, using bins of equal width. To show the overall trends in the data, for every gene, we fit the expression (UMI counts, scaled log-normalized expression, scaled Pearson residuals) as a function of  $\log_{10}$ -transformed mean UMI count using kernel regression (`ksmooth` function) with normal kernel and large bandwidth (20 times the size suggested by R function `bw.SJ`). For visualization, we only used the central 90% of cells based on total UMI. For every gene group, we show the expression range after smoothing from first to third quartile at 200 equidistant cell UMI values.

### Simulation study to assess sensitivity of variable gene detection

To evaluate the sensitivity of our method to detect variable genes, we used simulated data. The goal of our simulation was to generate two populations of cells (A and B, 5k cells each), while introducing expression shifts between



groups to some of the genes. To get a realistic set of model parameters, we first chose a group of cells (FCGR3A+, MS4A7+ Monocytes; 2924 cells) from the main 33k-cell PBMC dataset to learn a regularized NB model for each gene (ca. 12k genes). We then randomly chose 5% of the genes to have a higher mean in A vs B (ratio 10/1) and another 5% to have a lower mean in A vs B (ratio 1/10). Specifically, we adjusted the gene mean by a factor of  $\sqrt{10}$  in A (B) and  $\frac{1}{\sqrt{10}}$  in B (A) for genes that are high in A (B). We then adapted the model parameters (intercept, slope, theta) based on the new gene mean and the regularization curve learned from real data. Genes not selected to be variable had identical mean and model parameters in A and B.

We generated count data by first sampling a total cell UMI count from the input data (2924 Monocytes, see above). Given the total UMI, we could obtain the NB mean parameters for each gene per cell group (A and B), and together with the gene-specific theta generate UMI counts. This procedure was repeated 5k times, each time generating a cell for groups A and B. The combined count matrix of 10k cells was then used as input to our normalization method.

Finally, we repeated the above procedure 13 times and summarized the results in Additional file 2: Figure S6, specifically looking at the Jensen-Shannon divergence of the generating models and the variance of the Pearson residuals.

### Variance contribution analysis

To evaluate whether gene variance is dependent on sequencing depth, we determined the contribution of different cell groups to the overall variance of our six previously determined gene sets. For this, we placed all cells into five equal-sized groups based on total UMI counts (group 1 has the greatest depth, group 5 the lowest). We center each gene and square the values to obtain the squared deviation from the mean. The variance contribution of a cell group is then the sum of the values in those cells divided by the sum across all cells.

### Density maps for Pearson residuals

To illustrate different models (regularized NB, Poisson, non-regularized NB) for four example genes, we show Pearson residuals on  $256 \times 256$  grids in form of heatmaps. *X*- and *Y*-axis ranges were chosen to represent the central 98% of cells and central 99.8% of UMI counts. Heatmap colors show the magnitude (absolute value) of Pearson residuals, clipped to a maximum value of 4.

### Dimensionality reduction

For both log-normalized data and Pearson residuals, we performed dimensionality reduction as follows. We centered and scaled all 16K genes, clipped all values to the

interval  $[-10, 10]$  and performed a truncated principal components analysis as provided by the `irlba` R package. In both cases, we kept the first 25 PCs based on eigenvalue drop-off. For 2D visualization, the PC embeddings were passed into UMAP [36, 37] with default parameters.

### Differential expression testing

Differential expression testing was done using independent *t* tests per gene for all genes detected in at least 5 cells in at least one of the two groups being compared. *P* values were adjusted for multiple comparisons using the Benjamini and Hochberg method (FDR). Input to the test was either log-normalized ( $\log(10,000 \text{UMI}_{\text{gene}}/\text{UMI}_{\text{cell}} + 1)$ ) expression or Pearson residuals after regularized NB regression. A random background distribution of mean differences was generated by randomly choosing 1000 genes and permuting the group labels. Significance thresholds for the difference of means were derived from the background distribution by taking the 0.5th and 99.5th percentile. Finally, we called genes differentially expressed if the FDR was below 0.01 and the difference of means exceeded the threshold for significance.

### Model extensions—additional nuisance parameters

For the results shown in this manuscript, we have used the log-transformed total number of UMI assigned to each cell as the dependent variable to model gene-level UMI counts. However, other variables may also be suitable as long as they capture the sampling depth associated with each cell.

Additionally, the model can be flexibly extended to include additional covariates representing nuisance sources of variation, including cell-cycle state, mitochondrial percentage, or experimental batch. In these cases (unlike with sequencing depth), no regularization can be performed for parameters involving these variables, as genes with similar abundances cannot be assumed to (for example) be expressed in a similar pattern across the cell cycle. In these cases, we first learn regularized models using only the sequencing depth covariate, as described above. We next perform a second round of NB regression, including both the depth covariate and additional nuisance parameters as model predictors. In this round, the depth-dependent parameters are fixed to their previously regularized values, while the additional parameters are unconstrained and fit during the regression. The Pearson residuals of this second round of regression represent normalized data.

As a proof-of-concept, we illustrate a potential model extension by including a batch indicator variable when analyzing a dataset of 26,439 murine bipolar cells produced by two experimental batches [32], considering all bipolar cells and Müller glia. After running `sctransform`, either with the inclusion or exclusion of



the batch covariate, we performed PCA on all genes and used the first 20 dimensions to compute a UMAP embedding (Additional file 2: Figure S8). We include this example as a demonstration for how additional nuisance parameters can be included in the GLM framework, but note that when cell-type-specific batch effects are present, or there is a shift in the percentage of cell types across experiments, non-linear batch effect correction strategies are needed [18].

## Supplementary information

**Supplementary information** accompanies this paper at <https://doi.org/10.1186/s13059-019-1874-1>.

- Additional file 1:** Application of sctransform to additional UMI datasets.
- Additional file 2:** Supplementary figures.
- Additional file 3:** Guide to using sctransform in Seurat.
- Additional file 4:** Review history.

## Peer review information

Barbara Cheifet was the primary editor of this article and managed its editorial process and peer review in collaboration with the rest of the editorial team.

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## Review history

The review history is available as Additional file 4.

## Authors' contributions

CH and RS conceived of the method, derived the models, performed the experiments, and analyzed the data. Both authors discussed the results and wrote the final manuscript. Both authors read and approved the final manuscript.

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## Availability of data and materials

The dataset used in the main text is "33k PBMCs from a Healthy Donor, v1 Chemistry" from 10x Genomics (licensed under the Creative Commons Attribution license; also made available in our OSF project <https://osf.io/49mjf>). Additional datasets used in the study are listed in Additional file 1, along with GEO accession numbers and download links. Software implementing our approach is freely available as an open-source R package `scTransform`. We have deposited the source code in an OSF project under GPL-3.0 license [38]. For active development, we use GitHub [39] ([github.com/ChristophH/scTransform](https://github.com/ChristophH/scTransform)). A vignette showing the use of `scTransform` in Seurat v3 is also provided (Additional file 3).

## Ethics approval and consent to participate

Not applicable.

## Competing interests

The authors declare that they have no competing interests.

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